

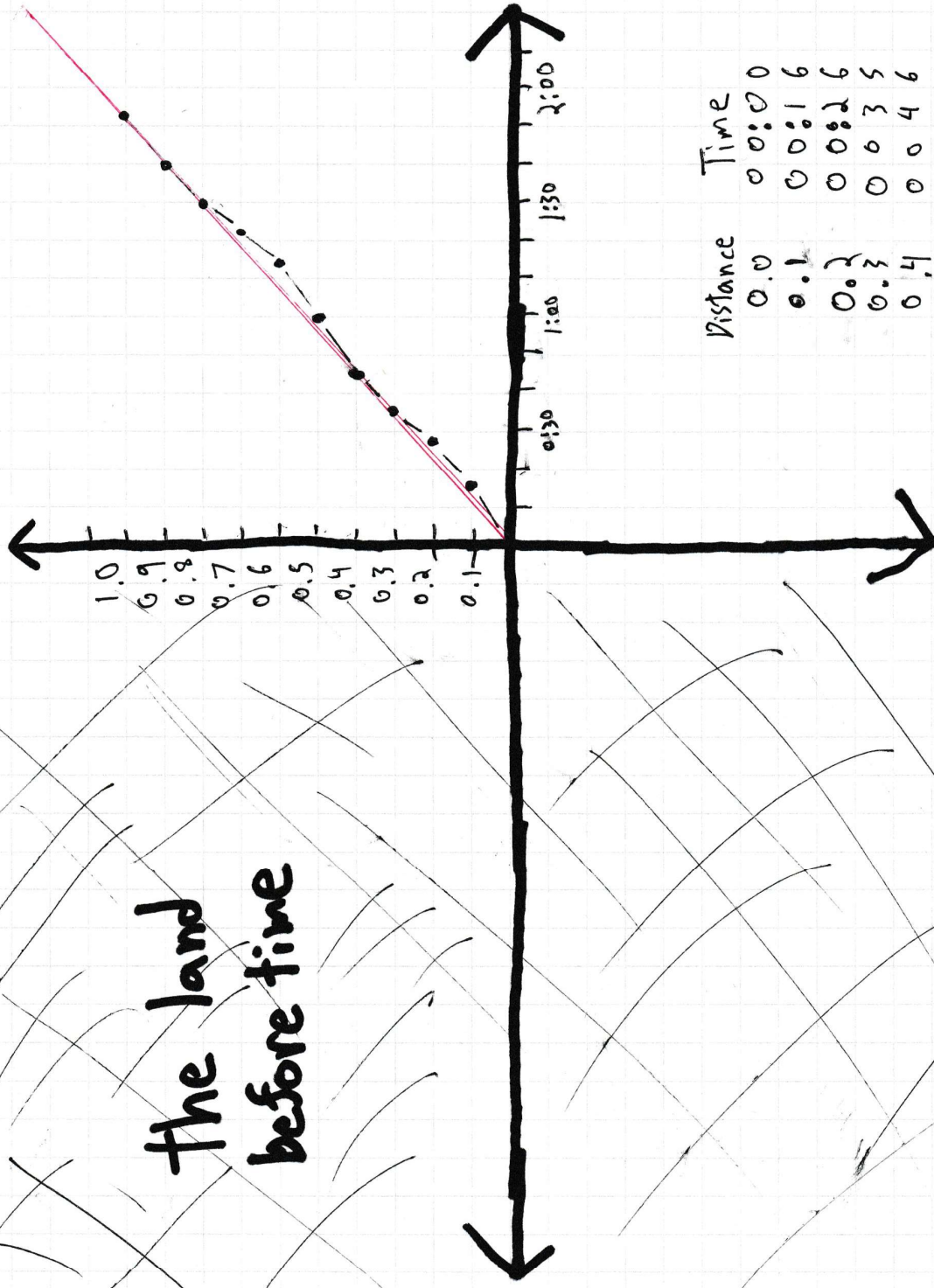
$$60 \frac{\text{km}}{\text{hr}} \cdot (0:15 \text{ min}) = 60 \times 0.25$$

$$= 15 \text{ km}$$

$$30 \frac{\text{km}}{\text{hr}} \cdot (0:15) = 30 \cdot 0.25 = 7.5 \text{ km} \uparrow$$

now what?

the land
before time



Distance	Time
0.0	0:00
0.1	0:16
0.2	0:32
0.3	0:48
0.4	1:04
0.5	1:20
0.6	1:36
0.7	1:52
0.8	2:08
0.9	2:24
1.0	2:40

Distance

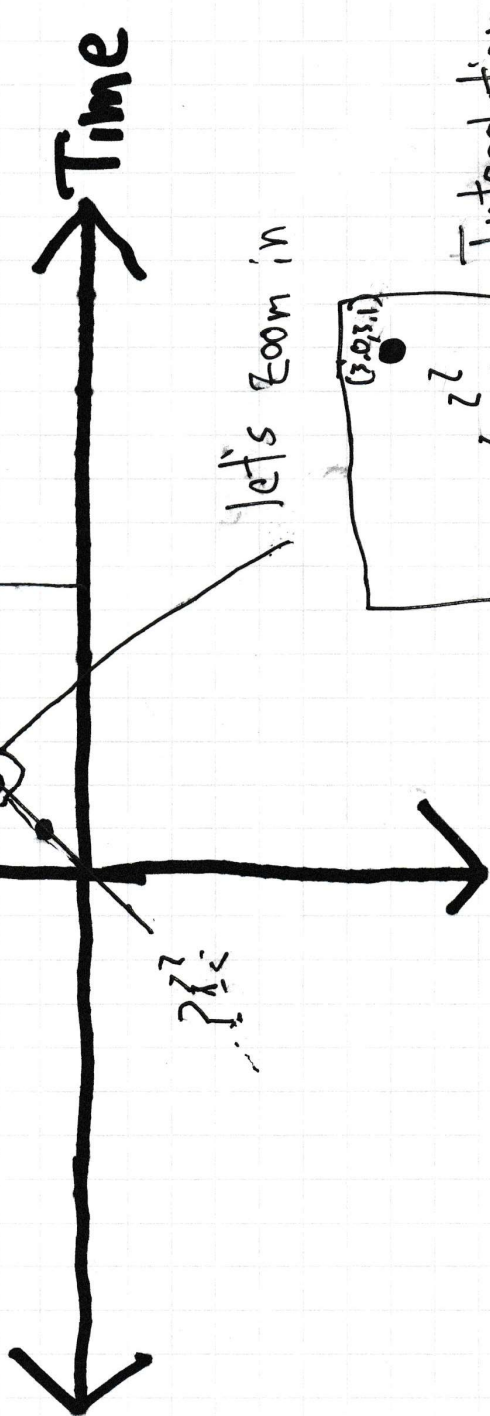
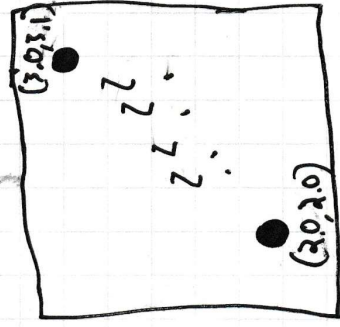
Time

Extrapolation

Intepolation

let's zoom in

Data



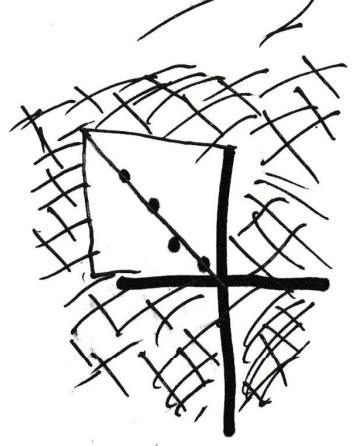
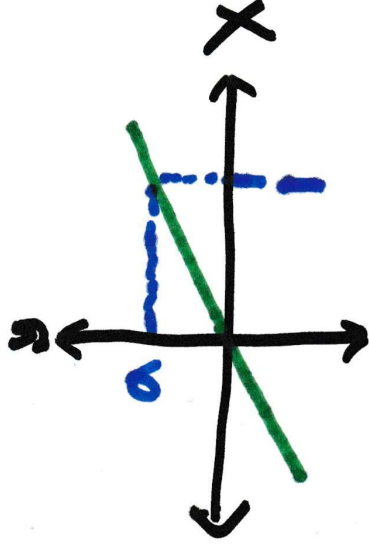
Position/distance

from some starting
point such that

the distance is proportional
to the time elapsed multiplied

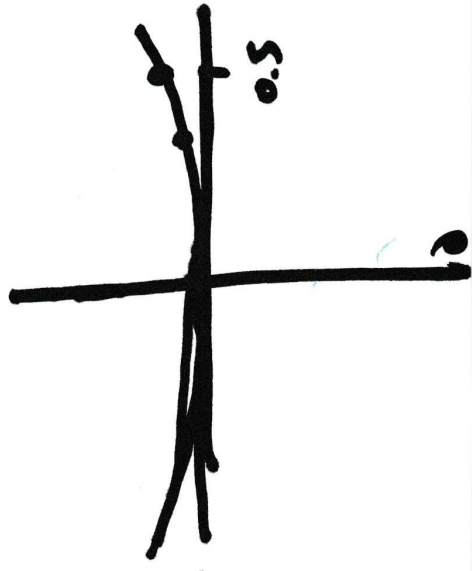
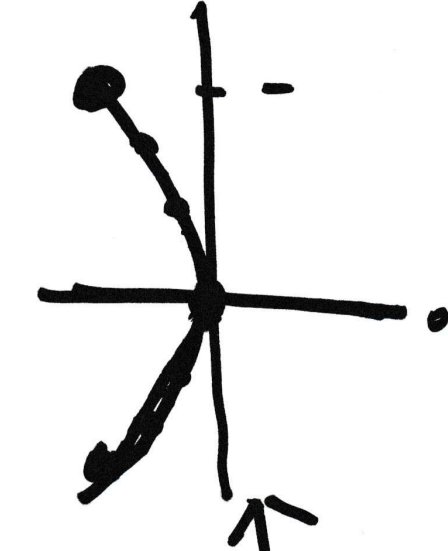
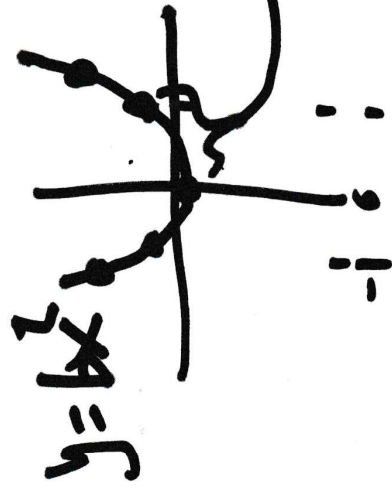
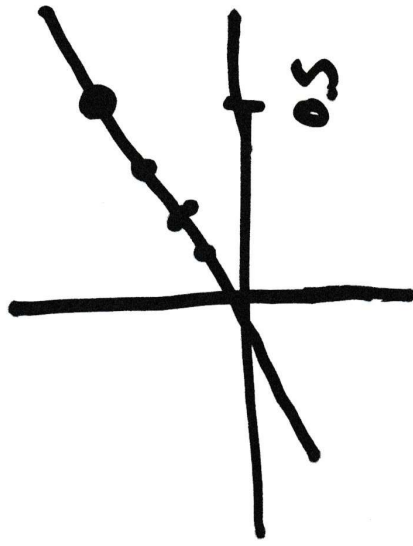
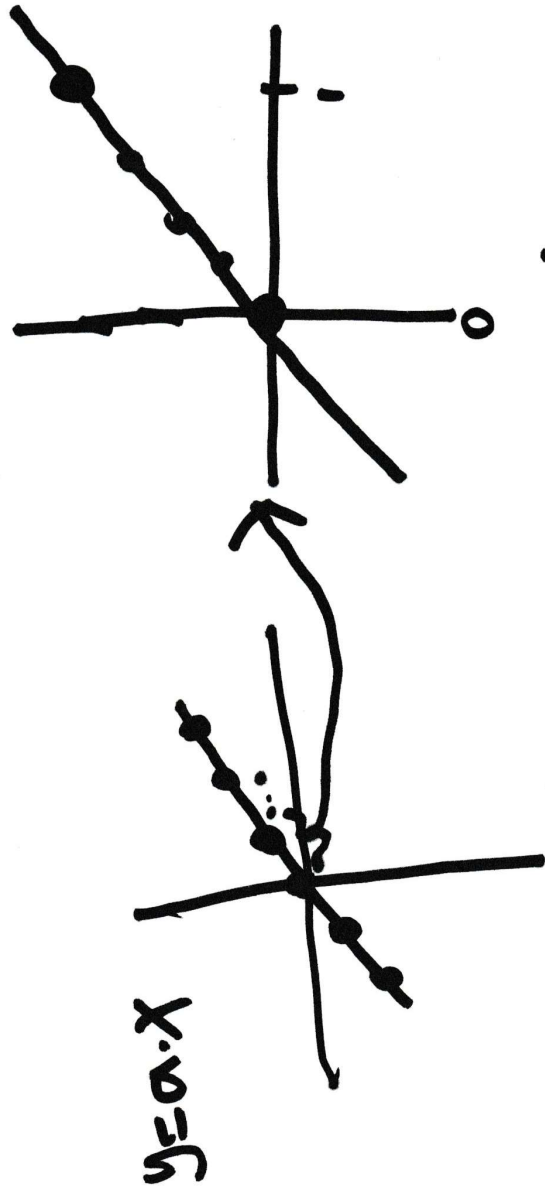
by the velocity in the relevant
units

$$y = f(x) = a \cdot x$$



$$d = s \cdot t$$

$y(x)$ is just math, no data,
 can keep zooming in



$y = f(x) = y(x)$ = mathematical
operations which
can be done with
Variable "x"
to get
"y"

distance(time) = $Z(t)$

Can we calculate an object's position
using the time Since we last knew
where it was? yes we can!!
xxx

...
with new events

$d^2 \quad z^2 \quad x^2 \quad y^2 \quad \dots$

or even $\vec{X} = (x, y, z)$
for today

$d = \text{distance} = \text{scalar}$

$t = \text{time}$

$$d = st$$

simplest

$$d = ct^2$$

$$d = bt^3$$

$$d = at^4$$

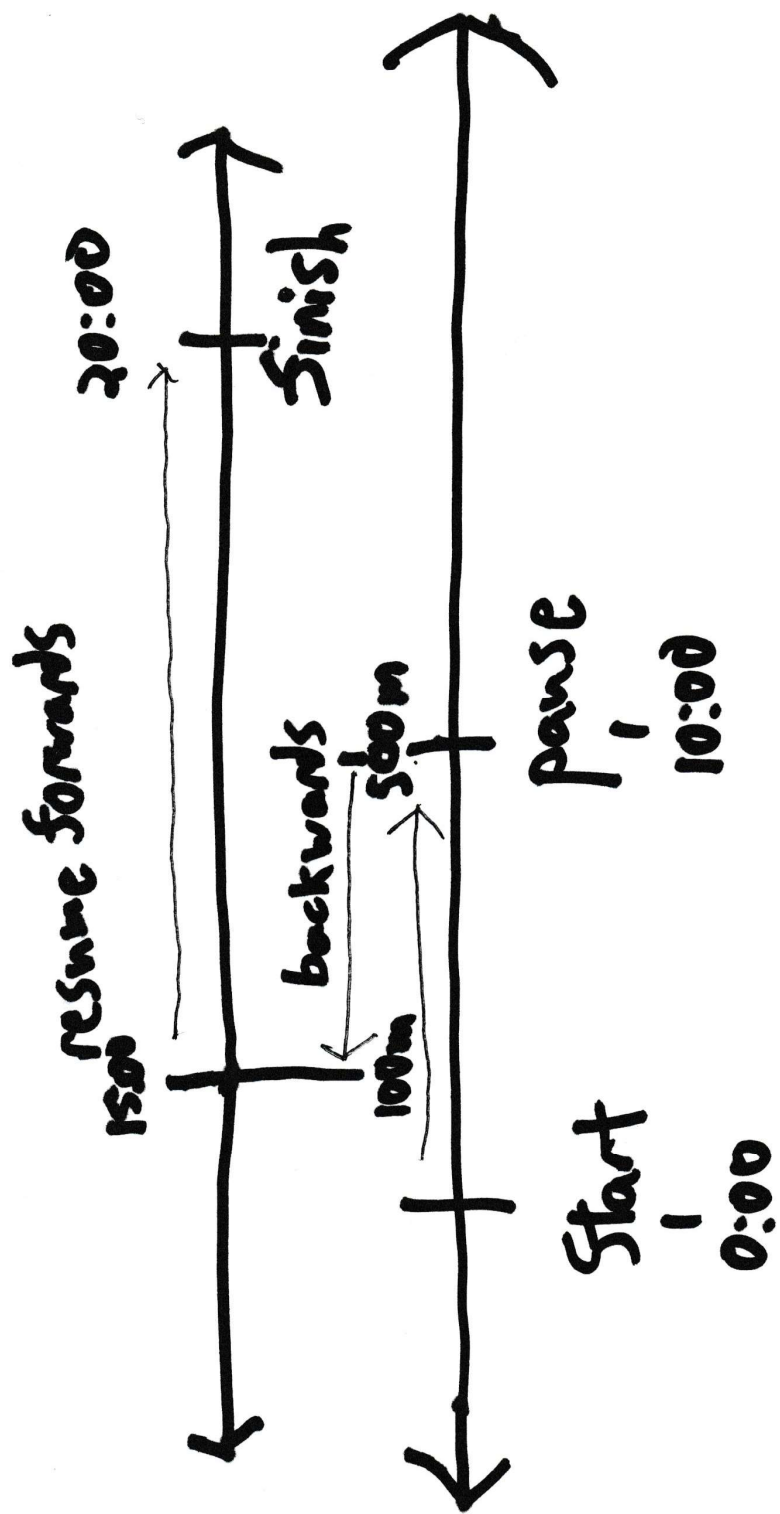
or even

$$d = \sin(t) \cdot a$$

$$d = \cos(t+s) \cdot b + c$$

$$d = e^{-x}$$

... etc

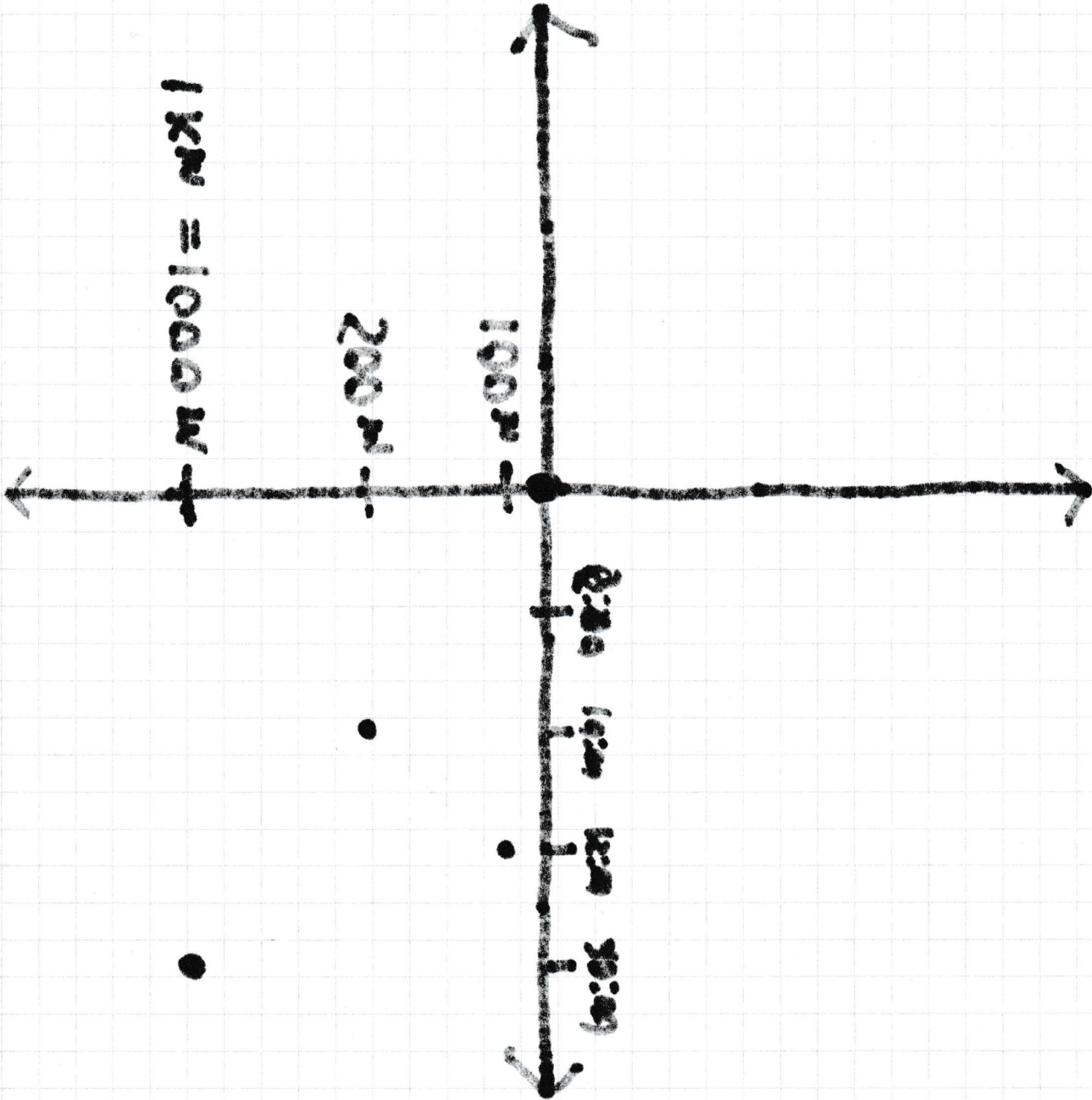


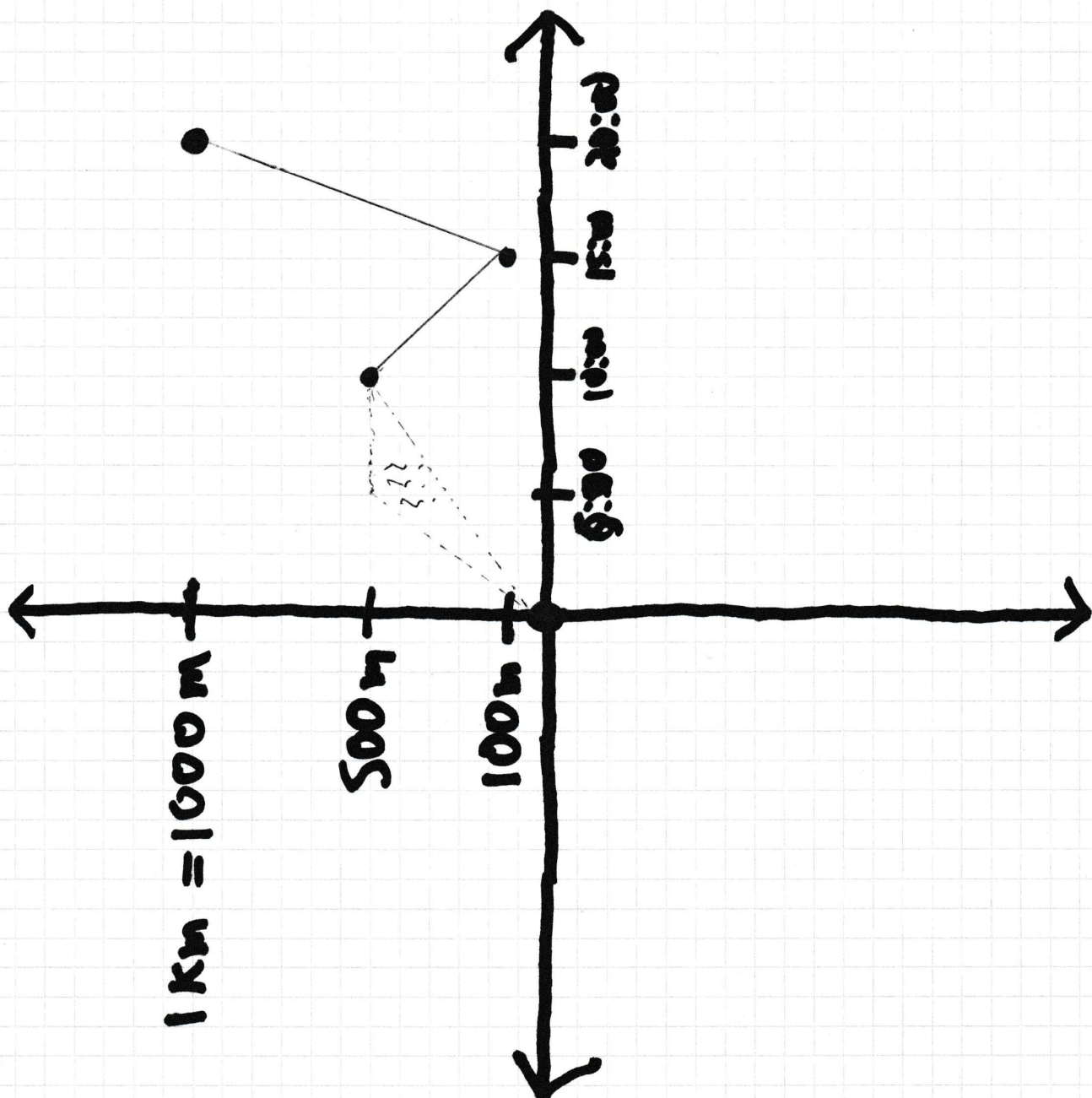
FIVE STAR.
★★★★★

FIVE STAR.
★★★★★

FIVE STAR.
★★★★★

FIVE STAR.
★★★★★





but $\text{speed} \equiv \frac{\text{distance}}{\text{time}} \neq \text{constant}$

Speed? $\downarrow$

$$d = 2 \cdot t = \frac{22}{1} \quad \frac{4}{2} \quad \frac{6}{3} \quad \frac{8}{4}$$

22 2 2 2

Speed? $\downarrow$

$$d = 2 \cdot t^2 = \frac{22}{1} \quad \frac{8}{2} \quad \frac{18}{3} \quad \frac{32}{4}$$

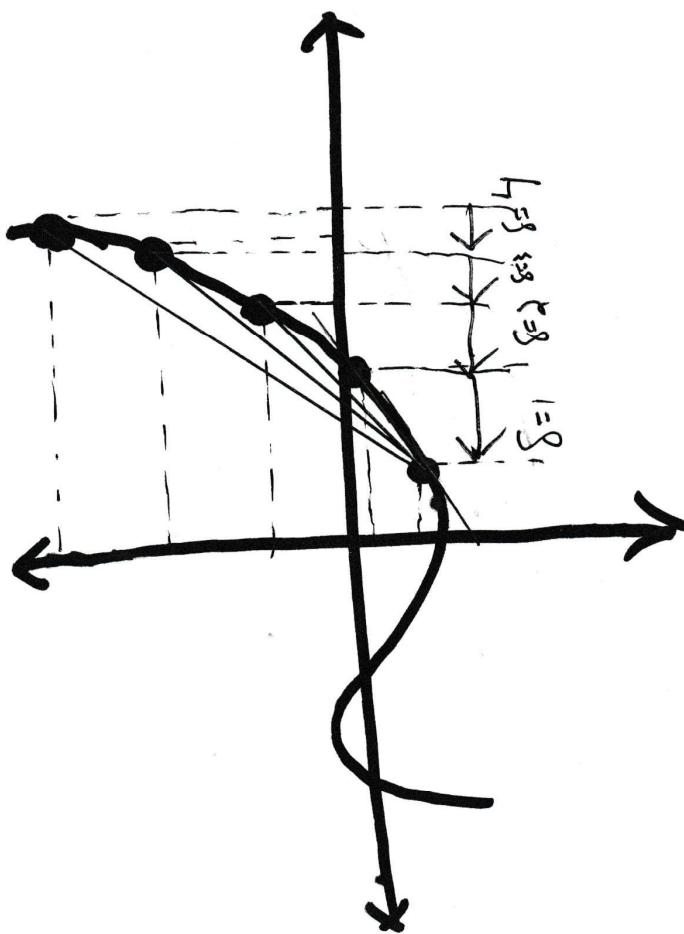
22 4 9 16

let's define

" $\frac{d}{dx}$ " the derivative

$$\boxed{\frac{d}{dx} f(x) = f'(x)} \rightarrow \frac{d}{dt} f(t) = \dot{f}(t) \quad \text{for time only}$$

$$\frac{d}{dx} f(x) = \lim_{\delta \rightarrow 0} \frac{f(x+\delta) - f(x)}{\delta}$$



$$y = a \cdot x \quad \text{is easy}$$

$$f(x) = a \cdot x \rightarrow \frac{d}{dx} f(x) = \frac{a(x+\delta) - a \cdot x}{\delta} = \frac{\cancel{ax} + a\delta}{\delta}$$

$$= a$$

$$f(x) = b x^2 \rightarrow \frac{d}{dx} f(x) = \frac{b \cdot (x+\delta)^2 - b x^2}{\delta}$$

$$= \frac{bx^2 - bx^2 + 2bx\delta + b\delta^2}{\delta} = 2bx + b\delta \xrightarrow{\delta \rightarrow 0} 2bx = 2 \cdot b \cdot x$$

